

## Normal Vibrations and Thermodynamic Properties of Chromium and Molybdenum Hexacarbonyls

By Kiyoyasu KAWAI and Hiromu MURATA

(Received December 4, 1959)

Hawkins, Mattraw, Sabol and Carpenter<sup>1)</sup> have observed successfully infrared spectra of chromium and molybdenum hexacarbonyls in gaseous state and have made an attempt to obtain Raman spectra of molybdenum hexacarbonyl. Recently, Danti and Cotton<sup>2)</sup> have reported Raman spectra of those and tungsten hexacarbonyls using chloroform as solvent. The molecular structure by electron diffraction has been reported by Brockway, Evens and Lister<sup>3)</sup>, and by X-ray diffraction by Rudolf and Fofmann<sup>4)</sup>, and it has been clear for the molecule to have  $O_h$ -symmetry. The assignments of the observed frequencies have been made by these investigators and the thermodynamic properties have been calculated by Hawkins, Mattraw, Sabor and Carpenter<sup>1)</sup>.

Out of thirteen fundamental vibrations resulting from the  $O_h$ -symmetry of the  $M(XY)_6$  type of molecule only four fundamental vibrations are infrared active, and the lowest frequency of them, which has considerably great contribution to thermodynamic properties is out of the region of the observation by a usual spectrometer. In connection with the other metal carbonyls previously reported<sup>5)</sup> and now proceeding\*, the present paper\*\* deals with a normal coordinate analysis for chromium and molybdenum hexacarbonyls to establish the more reliable assignments of vibrational frequencies and to compute the potential constants which may afford some information concerning the nature of the metal-carbonyl and carbonyl bonds in those compounds. The thermodynamic properties based on these assignments were calculated.

### Normal Coordinate Treatment

The method of group theory shows that, as explained by Hawkins, Mattraw, Sabol and Carpenter<sup>1)</sup>, thirty-three normal modes of vibration of the octahedral  $M(XY)_6$  type molecule are reduced to two of  $a_{1g}$ , two of  $e_g$ , one of  $f_{1g}$ , four of  $f_{1u}$ , two of  $f_{2g}$  and two of  $f_{2u}$ , and  $a_{1g}$ ,  $e_g$  and  $f_{2g}$  species are active in Raman and  $f_{1u}$  species in infrared. The  $f_{1g}$  and  $f_{2u}$  species are inactive in both.

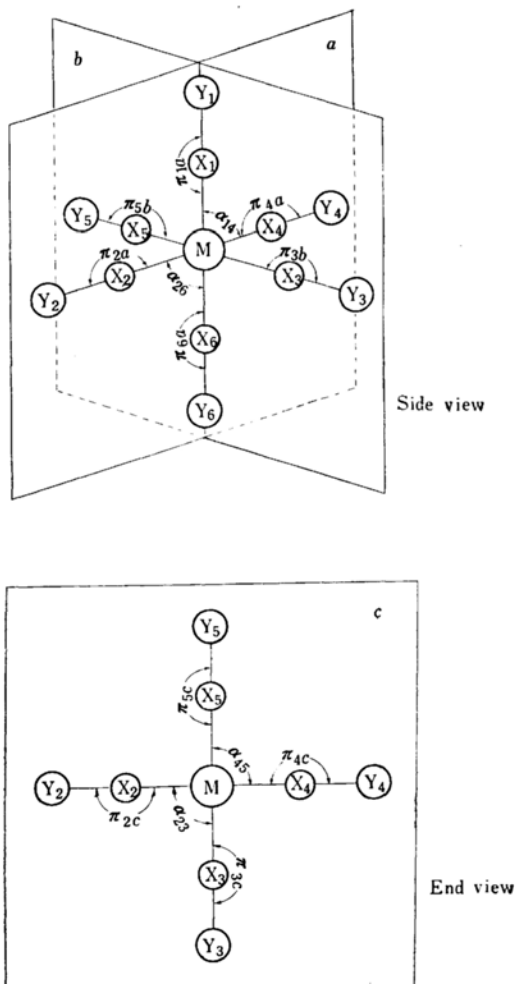


Fig. 1. Internal coordinates of  $M(XY)_6$  molecule.

1) N. J. Hawkins, H. C. Mattraw, W. W. Sabol and D. R. Carpenter, *J. Chem. Phys.*, **23**, 2422 (1955).

2) A. Danti and F. A. Cotton, *ibid.*, **28**, 736 (1958).

3) L. O. Brockway, R. V. G. Evens and M. W. Lister, *Trans. Faraday Soc.*, **34**, 1350 (1938).

4) W. Rudolf and U. Fofmann, *Z. physik Chem.*, **B28**, 351 (1935).

5) H. Murata and K. Kawai, *J. Chem. Phys.*, **26**, 1355 (1957); K. Kawai and H. Murata, *J. Chem. Soc. Japan, Pure Chem. Sec. (Nippon Kagaku Zasshi)*, **78**, 496 (1957).

\* A normal coordinate treatment of iron pentacarbonyl is being carried out in our laboratory. A part of the study has already been reported by H. Murata and K. Kawai, *J. Chem. Phys.*, **28**, 516 (1958).

\*\* A part of this work has been reported by H. Murata and K. Kawai, *J. Chem. Phys.*, **27**, 605 (1957).

The general secular equation may be obtained by means of the Wilson's method<sup>6)</sup>. The internal coordinates of  $M(XY)_6$  molecule of this type are as follows:

$$\begin{aligned} d(M-X_i) &= x_i & d(X_i-Y_i) &= y_i \\ \angle(M-X_i-Y_i) \text{ lying in } j\text{th plane} &= \pi_{ij} \\ \angle(X_i-M-X_j) &= \alpha_{ij} \end{aligned}$$

Fig. 1 illustrates the above internal coordinates.

The symmetry coordinates were set up from these internal coordinates as follows:

For  $a_{1g}$  species:

$$\begin{aligned} R_1 &= 1/\sqrt{6} (\Delta y_1 + \Delta y_2 + \Delta y_3 + \Delta y_4 \\ &\quad + \Delta y_5 + \Delta y_6) \\ R_2 &= 1/\sqrt{6} (\Delta x_1 + \Delta x_2 + \Delta x_3 + \Delta x_4 \\ &\quad + \Delta x_5 + \Delta x_6) \end{aligned}$$

For  $e_g$  species:

$$\begin{aligned} R_{3a} &= 1/\sqrt{12} (2\Delta y_1 - \Delta y_2 - \Delta y_3 - \Delta y_4 \\ &\quad - \Delta y_5 + 2\Delta y_6) \\ R_{4a} &= 1/\sqrt{12} (2\Delta x_1 - \Delta x_2 - \Delta x_3 - \Delta x_4 \\ &\quad - \Delta x_5 + 2\Delta x_6) \end{aligned}$$

For  $f_{1g}$  species:

$$R_{5a} = 1/2 (\Delta \pi_{1a} - \Delta \pi_{2a} + \Delta \pi_{4a} - \Delta \pi_{6a})$$

For  $f_{1u}$  species:

$$\begin{aligned} R_{6a} &= 1/2 (\Delta y_1 + \Delta y_2 - \Delta y_4 - \Delta y_6) \\ R_{7a} &= 1/\sqrt{8} (\Delta \pi_{1a} + \Delta \pi_{2a} + \Delta \pi_{3b} - \Delta \pi_{3c} \\ &\quad + \Delta \pi_{4a} + \Delta \pi_{5b} + \Delta \pi_{5c} + \Delta \pi_{6a}) \\ R_{8a} &= 1/2 (\Delta x_1 + \Delta x_2 - \Delta x_4 - \Delta x_6) \\ R_{9a} &= 1/4 (2\Delta \alpha_{12} + \Delta \alpha_{13} + \Delta \alpha_{15} + \Delta \alpha_{23} + \Delta \alpha_{25} \\ &\quad - \Delta \alpha_{34} - \Delta \alpha_{36} - \Delta \alpha_{45} - \Delta \alpha_{56} - 2\Delta \alpha_{46}) \end{aligned}$$

For  $f_{2g}$  species:

$$\begin{aligned} R_{10a} &= 1/2 (\Delta \pi_{1a} + \Delta \pi_{2a} - \Delta \pi_{4a} - \Delta \pi_{6a}) \\ R_{11a} &= 1/2 (\Delta \alpha_{12} - \Delta \alpha_{14} - \Delta \alpha_{26} + \Delta \alpha_{46}) \end{aligned}$$

For  $f_{2ua}$  species:

$$\begin{aligned} R_{12a} &= 1/\sqrt{8} (\Delta \pi_{1a} + \Delta \pi_{2a} - \Delta \pi_{3b} + \Delta \pi_{3c} \\ &\quad + \Delta \pi_{4a} - \Delta \pi_{5b} - \Delta \pi_{5c} + \Delta \pi_{6a}) \\ R_{13a} &= 1/4 (2\Delta \alpha_{12} - \Delta \alpha_{13} - \Delta \alpha_{15} - \Delta \alpha_{23} - \Delta \alpha_{25} \\ &\quad + \Delta \alpha_{34} + \Delta \alpha_{36} + \Delta \alpha_{45} + \Delta \alpha_{56} - 2\Delta \alpha_{46}) \end{aligned}$$

Using the table of Decius<sup>7)</sup> and for the  $M-X-Y$  bending the method by Ferigle and Meister<sup>8)</sup>  $G$  matrices were evaluated. In terms of the abbreviations  $\rho$  and  $\tau$  for reciprocal of the bond lengths  $x$  and  $y$ , respectively, and  $\mu_M$ ,

$\mu_X$  and  $\mu_Y$  for the reciprocals of the atomic masses, the following  $G$  matrix elements were obtained\*\*\*:

For  $a_{1g}$  species:

$$G_{11} = \mu_X + \mu_Y, \quad G_{12} = -\mu_X, \quad G_{22} = \mu_X$$

For  $e_g$  species:

$$\begin{aligned} G_{33} &= G_{11}(a_{1g}), \quad G_{34} = G_{12}(a_{1g}), \\ G_{44} &= G_{22}(a_{1g}) \end{aligned}$$

For  $f_{1g}$  species:

$$G_{55} = (\rho + \tau)^2 \mu_X + \tau^2 \mu_Y$$

For  $f_{1u}$  species:

$$\begin{aligned} G_{66} &= G_{11}(a_{1g}), \quad G_{67} = G_{69} = 0, \\ G_{68} &= G_{12}(a_{1g}), \\ G_{77} &= 4\rho^2 \mu_M + (\rho + \tau)^2 \mu_X + \tau^2 \mu_Y, \\ G_{78} &= \sqrt{8} \rho \mu_M, \\ G_{79} &= -\sqrt{2} \{4\rho^2 \mu_M + (\rho^2 + \rho\tau) \mu_X\}, \\ G_{88} &= 2\mu_M + \mu_X, \quad G_{89} = -4\rho \mu_M, \\ G_{99} &= 2\rho^2 (4\mu_M + \mu_X) \end{aligned}$$

For  $f_{2g}$  species:

$$\begin{aligned} G_{1010} &= G_{55}(f_{1g}), \\ G_{1011} &= -2(\rho^2 + \rho\tau) \mu_X, \quad G_{1111} = 4\rho^2 \mu_X \end{aligned}$$

For  $f_{2u}$  species:

$$\begin{aligned} G_{1212} &= G_{55}(f_{1g}), \\ G_{1213} &= -\sqrt{2} (\rho^2 + \rho\tau) \mu_X, \\ G_{1313} &= 2\rho^2 \mu_X \end{aligned}$$

Following the method of Shimanouchi<sup>9)</sup>, the Urey-Bradley type quadratic potential energy function for octahedral  $M(XY)_6$  molecule may be written as:

$$\begin{aligned} 2V &= \sum_{i=1}^6 \{K(M-X) + 2[F(X \cdots X) \\ &\quad + F^I(X \cdots X)]\} (\Delta x_i)^2 \\ &\quad + \sum_{i=1}^6 K(X-Y) (\Delta y_i)^2 \\ &\quad + \sum_{i < j=1}^6 \{H(X-M-X) + 1/2 [F(X \cdots X) \\ &\quad - F^I(X \cdots X)]\} (x_0 \Delta \alpha_{ij})^2 \\ &\quad + \sum_{i=1}^6 \sum_{l=a}^c H(M-X-Y) (\sqrt{x_0 y_0} \Delta \pi_{il})^2 \\ &\quad + 2 \sum_{i < j=1}^6 1/2 [F(X \cdots X)] \end{aligned}$$

\*\*\* There is one misprint in the  $G$  matrix elements presented by H. Murata and K. Kawai, *J. Chem. Phys.*, **26**, 605 (1957), viz  $G_{24}$  in  $f_{1u}$  species which corresponds to  $G_{79}$  of this paper.

9) T. Shimanouchi, *J. Chem. Phys.*, **17**, 245, 734, 848 (1949).

6) E. B. Wilson, Jr., *J. Chem. Phys.*, **7**, 1047 (1939), **9**, 76 (1941).

7) J. C. Decius, *ibid.*, **16**, 1025 (1948).

8) S. M. Ferigle and A. G. Meister, *ibid.*, **19**, 982 (1951).

$$\begin{aligned}
& -F'(X\cdots X)(\Delta x_i)(\Delta x_j) \\
& + 2 \sum_{i < j=1}^6 1/2 [F(X\cdots X) \\
& + F'(Y\cdots X)(\Delta x_i)(x_0 \Delta \alpha_{ij}) \\
& + 2 \sum_{i \approx j \approx k=1}^6 1/(2x_0^2) \kappa(x_0 \Delta \alpha_{ij})(x_0 \Delta \alpha_{ik})
\end{aligned}$$

where  $x_0$  and  $y_0$  are the equilibrium M—X and X—Y bond distances respectively;  $K$ ,  $H$ ,  $F$  and  $F'$  are the potential constants and  $\kappa$  the intra-molecular tension whose definition and physical meaning were expressed by Shimanouchi<sup>9</sup>.

The intra-molecular tension for the octahedral  $MX_6$  type molecule can easily be derived from the following relation obtained for the octahedral geometrical structure

$$\sum (\Delta \alpha_{ij}) + 1/2 \sum (\Delta \alpha_{ij})(\Delta \alpha_{ik}) = 0$$

where the first summation extends for all of the twelve angles and the second for all the forty-eight sets of adjacent angles.

The potential energy matrix elements evaluated from the above potential function are as follows:

For  $a_{1g}$  species:

$$F_{11} = K(X-Y), \quad F_{12} = 0,$$

$$F_{22} = K(M-X) + 4F(X\cdots X)$$

For  $e_g$  species:

$$F_{33} = F_{11}(a_{1g}), \quad F_{34} = 0,$$

$$F_{44} = K(M-X) + 0.7F(X\cdots X)$$

For  $f_{1g}$  species:

$$F_{55} = x_0 y_0 H(M-X-Y)$$

For  $f_{1u}$  species:

$$F_{66} = F_{11}(a_{1g}), \quad F_{77} = F_{55}(f_{1g}),$$

$$F_{88} = K(M-X) + 1.8F(X\cdots X),$$

$$F_{89} = 0.9x_0 F(X\cdots X),$$

$$F_{99} = x_0^2 [H(X-M-X) + 0.55F(X\cdots X)] + \kappa,$$

$$F_{67} = F_{68} = F_{69} = F_{78} = F_{79} = 0$$

For  $f_{2g}$  species:

$$F_{1010} = F_{55}(f_{1g}), \quad F_{1011} = 0,$$

$$F_{1111} = x_0^2 [H(X-M-X) + 0.55F(X\cdots X)]$$

For  $f_{2u}$  species:

$$F_{1212} = F_{55}(f_{1g}), \quad F_{1213} = 0,$$

$$F_{1313} = x_0^2 [H(X-M-X) + 0.55F(X\cdots X)] - \kappa$$

In the above elements it was assumed experimentally that  $F' = -1/10F$ , and consequently six potential constants are used here.

TABLE I. MOLECULAR CONSTANTS FOR  $Cr(CO)_6$  AND  $Mo(CO)_6$ <sup>a</sup>

| Bond              | $Cr(CO)_6$ | $Mo(CO)_6$ |
|-------------------|------------|------------|
| M <sup>b</sup> —C | 1.92 Å     | 2.08 Å     |
| C—O               | 1.16 Å     | 1.15 Å     |

Symmetry number.....24 for all fundamentals

a From Ref. 3.

b M denotes Cr or Mo.

TABLE II. POTENTIAL CONSTANTS FOR  $Cr(CO)_6$  AND  $Mo(CO)_6$  (mdyn./Å)

| Type           | $Cr(CO)_6$          | $Mo(CO)_6$          |
|----------------|---------------------|---------------------|
| $K(C-O)$       | 16.2                | 16.02               |
| $K(M-C)$       | 1.83                | 1.77                |
| $H(M-C-O)$     | 0.41                | 0.34                |
| $H(C-M-C)$     | 0.03                | 0.02                |
| $F(C\cdots C)$ | 0.15                | 0.12                |
| $\kappa(MC_6)$ | 0.02 Å <sup>2</sup> | 0.02 Å <sup>2</sup> |

TABLE III. COMPARISON OF OBSERVED AND CALCULATED FUNDAMENTALS FOR  $Cr(CO)_6$  AND  $Mo(CO)_6$

| Type       | Assignment    |                 | $Cr(CO)_6$        |                  | $Mo(CO)_6$        |                  |
|------------|---------------|-----------------|-------------------|------------------|-------------------|------------------|
|            | Fundamental   | Description     | Calc.             | Obs.             | Calc.             | Obs.             |
| $a_{1g}$ : | $\sigma_1$    | $\nu(C-O)$      | 2042              | 2108             | 2037              | 2131             |
|            | $\sigma_2$    | $\nu(M-C)$      | 374               | 393              | 361               | 379              |
| $e_g$ :    | $\sigma_3$    | $\nu(C-O)$      | 2031              | 2019             | 2029              | 2022             |
|            | $\sigma_4$    | $\nu(M-C)$      | 336               | 373              | 329               | 334              |
| $f_{1g}$ : | $\sigma_5$    | $\delta(M-C-O)$ | 564               | 539              | 524               | 477              |
| $f_{1u}$ : | $\sigma_6$    | $\nu(C-O)$      | 1992 <sup>c</sup> | 2000             | 1992 <sup>c</sup> | 2000             |
|            | $\sigma_7$    | $\delta(M-C-O)$ | 636               | 661              | 560               | 595              |
|            | $\sigma_8$    | $\nu(M-C)$      | 475               | 436              | 422               | 368              |
| $f_{2g}$ : | $\sigma_9$    | $\delta(C-M-C)$ | 113               | 102              | 95                | 80               |
|            | $\sigma_{10}$ | $\delta(M-C-O)$ | 608               | 598 <sup>b</sup> | 560               | 557 <sup>b</sup> |
|            | $\sigma_{11}$ | $\delta(C-M-C)$ | 111               | 90               | 101               | 80               |
| $f_{2u}$ : | $\sigma_{12}$ | $\delta(M-C-O)$ | 586               | 570 <sup>b</sup> | 541               | 517 <sup>b</sup> |
|            | $\sigma_{13}$ | $\delta(C-M-C)$ | 81                | 80               | 72                | 70               |

a Obtained from the values of the L matrix elements.

b Inferred from combination or overtone bands.

c Obtained by the method of high-frequency separation.

To evaluate numerically the above elements, the bond lengths listed in Table I and the atomic masses on a physical scale were used.

### Discussion

A comparison of the normal frequencies calculated from the set of potential constants in Table II with those observed by Hawkins, Matraw, Sabol and Carpenter<sup>1)</sup> are summarized in Table III. The numbering of the frequencies is the same as that used by Hawkins et al.<sup>1)</sup>

The agreement between the calculated and the observed frequencies is satisfactory except for the M—C—O bending vibrations. The present results from the Urey-Bradley type potential function in which all the M—C—O

TABLE IV. INFRARED BANDS OF GASEOUS  
Cr(CO)<sub>6</sub>

| Frequency<br>(cm <sup>-1</sup> ) | Intensity | Assignment  | Calc.<br>(cm <sup>-1</sup> ) |
|----------------------------------|-----------|---|------------------------------|
| 4098                             | m         | $\sigma_1 + \sigma_6$                               | 4108                         |
| 4000                             | m         | $\sigma_3 + \sigma_6$                               | 4019                         |
| 2688                             | w         | $\sigma_3 + \sigma_7$                               | 2680                         |
| 2554                             | w         | $\sigma_1 + \sigma_8, \sigma_5 + \sigma_6$          | 2544, 2539                   |
| 2466                             | m         | $\sigma_3 + \sigma_8$                               | 2455                         |
| 2393                             | s         | $\sigma_2 + \sigma_6$                               | 2393                         |
| 2336                             | sh        | q   |                              |
| 2212                             | w         | $\sigma_1 + \sigma_9$                               | 2210                         |
| 2174                             | w         | q   |                              |
| 2121                             | s         | $\sigma_3 + \sigma_9$                               | 2121                         |
| 2090                             | s         | $\sigma_6 + \sigma_{11}, \sigma_3 + \sigma_{13}$    | 2090, 2099                   |
| 2033                             | sh        | q   |                              |
| 2000                             | vs        | $\sigma_6$  |                              |
| 1970                             | sh        | q   |                              |
| 1912                             | m         | $\sigma_3 - \sigma_9, \sigma_6 - \sigma_{11}$       | 1917, 1910                   |
| 1631                             | w         | $\sigma_6 - \sigma_4$                               | 1627                         |
| 1196                             | s         | $\sigma_5 + \sigma_7$                               | 1200                         |
| 1055                             | sh        | $\sigma_2 + \sigma_7$                               | 1054                         |
| 1032                             | s         | $\sigma_4 + \sigma_7, \sigma_8 + \sigma_{10}$       | 1034, 1034                   |
| 963                              | m         | $\sigma_5 + \sigma_8$                               | 975                          |
| 875                              | s         | q   |                              |
| 811                              | s         | $\sigma_4 + \sigma_8$                               | 809                          |
| 755                              | m         | $\sigma_7 + \sigma_{11}$                            | 751                          |
| 673                              | sh        | $\sigma_{10} + \sigma_{13}$                         | 678                          |
| 661                              | vs        | $\sigma_7$  |                              |
| 635                              | s (sh)    | $\sigma_5 + \sigma_9$                               | 641                          |
| 595                              | sh        | q   |                              |
| 522                              | mb        | $\sigma_8 + \sigma_{11}, \sigma_{10} - \sigma_{13}$ | 526, 518                     |
| 513                              | mb        | $\sigma_{10} - \sigma_{13}, \sigma_2 + \sigma_9$    | 518, 495                     |
| 477                              | mb        | $\sigma_4 + \sigma_9, \sigma_{12} - \sigma_{11}$    | 475, 480                     |
| 465                              | wb        | q   |                              |
| 449                              | wb        | $\sigma_4 + \sigma_{13}$                            | 453                          |
| 436                              | s         | $\sigma_8$  |                              |

vs Very strong; s Strong; m Medium; w Weak; b Broad; sh Shoulder; q More than binary combination or questionable band.

TABLE V. INFRARED BANDS OF GASEOUS  
Mo(CO)<sub>6</sub>

| Frequency<br>(cm <sup>-1</sup> ) | Intensity | Assignment                                       | Calc.<br>(cm <sup>-1</sup> ) |
|----------------------------------|-----------|--|------------------------------|
| 4150                             | m         | $\sigma_1 + \sigma_6$                            | 4131                         |
| 4050                             | m         | $\sigma_3 + \sigma_6$                            | 4022                         |
| 2600                             | w         | $\sigma_3 + \sigma_7$                            | 2617                         |
| 2480                             | w         | $\sigma_1 + \sigma_8, \sigma_5 + \sigma_6$       | 2499, 2477                   |
| 2380                             | s         | $\sigma_3 + \sigma_8, \sigma_2 + \sigma_6$       | 2390, 2379                   |
| 2330                             | w         | $\sigma_4 + \sigma_6$                            | 2334                         |
| 2210                             | m         | $\sigma_1 + \sigma_9$                            | 2211                         |
| 2115                             | s         | $\sigma_3 + \sigma_9$                            | 2102                         |
| 2085                             | s         | $\sigma_6 + \sigma_{11}, \sigma_3 + \sigma_{13}$ | 2080, 2092                   |
| 2000                             | vs        | $\sigma_6$                                       |                              |
| 1985                             | sh        | q  |                              |
| 1955                             | m (sh)    | $\sigma_3 - \sigma_{13}$                         | 1952                         |
| 1925                             | m (sh)    | $\sigma_6 - \sigma_{11}$                         | 1920                         |
| 1650                             | w         | $\sigma_3 - \sigma_8$                            | 1654                         |
| 1615                             | w         | $\sigma_6 - \sigma_2$                            | 1621                         |
| 1070                             | s         | $\sigma_5 + \rho_7, \sigma_{10} + \sigma_{12}$   | 1072, 1074                   |
| 980                              | s         | $\sigma_2 + \sigma_7$                            | 974                          |
| 927                              | s         | $\sigma_4 + \sigma_7, \sigma_8 + \sigma_{10}$    | 929, 925                     |
| 905                              | w         | q  |                              |
| 845                              | s         | $\sigma_5 + \sigma_8, \sigma_4 + \sigma_{12}$    | 845, 851                     |
| 740                              | m         | $\sigma_2 + \sigma_8$                            | 747                          |
| 705                              | m         | $\sigma_4 + \sigma_8$                            | 702                          |
| 670                              | m         | $\sigma_7 + \sigma_{11}$                         | 675                          |
| 661                              | w         | q  |                              |
| 595                              | vs        | $\sigma_7$                                       |                              |
| 563                              | s         | $\sigma_5 + \sigma_9$                            | 557                          |
| 386                              | s         | $\sigma_8$                                       |                              |

vs Very strong; s Strong; m Medium; w Weak; b Broad; sh Shoulder; q More than binary combination or questionable band.

bending interaction constants are not included indicated that 213 and 310 cm<sup>-1</sup> bands assigned to  $\sigma_{10}$  and  $\sigma_{12}$  respectively by Hawkins, Matraw, Sabol and Carpenter<sup>1)</sup> and 137.1 cm<sup>-1</sup> band to  $\sigma_{10}$  by Danti and Cotton<sup>2)</sup> for chromium hexacarbonyl and 230 and 327 cm<sup>-1</sup> bands by the former<sup>1)</sup> and 135.7 cm<sup>-1</sup> band by the latter<sup>2)</sup> for molybdenum hexacarbonyl are too small for M—C—O bending vibrational frequencies. Based on this point of view, all of the observed bands by Hawkins, Matraw, Sabol and Carpenter<sup>1)</sup> except for only three strong bands which may be designated as fundamentals, were reassigned as shown in Table IV for chromium hexacarbonyl and Table V for molybdenum hexacarbonyl.

In order to obtain better agreement with the observed frequencies of  $a_{1g}$  and  $e_g$  species some other sets of values of diagonal terms in F matrix were used, but as long as proper values with physical meaning were used the calculated values were not close to the observed ones. This, therefore, may suggest that the

TABLE VI. L MATRICES FOR  $\text{Cr}(\text{CO})_6$ 

|            |          | $Q_1$  | $Q_2$ | $Q_3$  | $Q_4$ | $Q_7$  | $Q_8$  | $Q_9$  | $Q_{10}$ | $Q_{11}$ | $Q_{12}$ | $Q_{13}$ |
|------------|----------|--------|-------|--------|-------|--------|--------|--------|----------|----------|----------|----------|
| $a_{1g}$ : | $R_1$    | 0.381  | 0.017 |        |       |        |        |        |          |          |          |          |
|            | $R_2$    | -0.226 | 0.187 |        |       |        |        |        |          |          |          |          |
| $e_g$ :    | $R_3$    |        |       | 0.380  | 0.012 |        |        |        |          |          |          |          |
|            | $R_4$    |        |       | -0.224 | 0.169 |        |        |        |          |          |          |          |
| $f_{1u}$ : | $R_7$    |        |       |        |       | 0.453  | -0.113 | 0.028  |          |          |          |          |
|            | $R_8$    |        |       |        |       | 0.120  | 0.242  | -0.007 |          |          |          |          |
|            | $R_9$    |        |       |        |       | -0.258 | -0.029 | 0.128  |          |          |          |          |
| $f_{2g}$ : | $R_{10}$ |        |       |        |       |        |        |        | 0.452    | 0.034    |          |          |
|            | $R_{11}$ |        |       |        |       |        |        |        | -0.274   | 0.123    |          |          |
| $f_{2u}$ : | $R_{12}$ |        |       |        |       |        |        |        |          |          | 0.453    | 0.017    |
|            | $R_{13}$ |        |       |        |       |        |        |        |          |          | -0.191   | 0.094    |

TABLE VII. L MATRICES FOR  $\text{Mo}(\text{CO})_6$ 

|            |          | $Q_1$  | $Q_2$ | $Q_3$  | $Q_4$ | $Q_7$  | $Q_8$  | $Q_9$  | $Q_{10}$ | $Q_{11}$ | $Q_{12}$ | $Q_{13}$ |
|------------|----------|--------|-------|--------|-------|--------|--------|--------|----------|----------|----------|----------|
| $a_{1g}$ : | $R_1$    | 0.382  | 0.015 |        |       |        |        |        |          |          |          |          |
|            | $R_2$    | -0.225 | 0.180 |        |       |        |        |        |          |          |          |          |
| $e_g$ :    | $R_3$    |        |       | 0.382  | 0.012 |        |        |        |          |          |          |          |
|            | $R_4$    |        |       | -0.224 | 0.182 |        |        |        |          |          |          |          |
| $f_{1u}$ : | $R_7$    |        |       |        |       | 0.451  | -0.044 | -0.021 |          |          |          |          |
|            | $R_8$    |        |       |        |       | 0.054  | 0.229  | 0.008  |          |          |          |          |
|            | $R_9$    |        |       |        |       | -0.021 | -0.034 | 0.110  |          |          |          |          |
| $f_{2g}$ : | $R_{10}$ |        |       |        |       |        |        |        | 0.445    | 0.031    |          |          |
|            | $R_{11}$ |        |       |        |       |        |        |        | -0.251   | 0.118    |          |          |
| $f_{2u}$ : | $R_{12}$ |        |       |        |       |        |        |        |          |          | 0.446    | 0.016    |
|            | $R_{13}$ |        |       |        |       |        |        |        |          |          | -0.175   | 0.090    |

TABLE VIII. HEAT CONTENT, FREE ENERGY, AND HEAT CAPACITY OF  $\text{Cr}(\text{CO})_6$  AND  $\text{Mo}(\text{CO})_6$  FOR THE IDEAL GASEOUS STATE AT 1 ATMOSPHERE (cal.  $\text{deg}^{-1} \text{mol}^{-1}$ )

| $T(^{\circ}\text{K})$ | $\text{Cr}(\text{CO})_6$ |                    |        | $\text{Mo}(\text{CO})_6$ |                   |                    |        |         |
|-----------------------|--------------------------|--------------------|--------|--------------------------|-------------------|--------------------|--------|---------|
|                       | $(H^0 - E_0^0)/T$        | $-(F^0 - E_0^0)/T$ | $S^0$  | $C_p^0$                  | $(H^0 - E_0^0)/T$ | $-(F^0 - E_0^0)/T$ | $S^0$  | $C_p^0$ |
| 273.15                | 28.99                    | 78.68              | 107.67 | 45.01                    | 30.77             | 82.65              | 113.42 | 48.24   |
| 298.15                | 30.48                    | 81.16              | 111.64 | 46.94                    | 32.28             | 85.43              | 117.71 | 49.08   |
| 300                   | 30.58                    | 81.35              | 111.93 | 47.06                    | 32.38             | 85.65              | 118.00 | 49.20   |
| 400                   | 35.52                    | 90.76              | 126.28 | 52.65                    | 37.25             | 95.63              | 132.88 | 54.17   |
| 600                   | 42.48                    | 106.49             | 148.97 | 59.20                    | 43.95             | 112.12             | 156.07 | 60.00   |
| 800                   | 47.24                    | 119.34             | 166.58 | 63.26                    | 48.49             | 125.45             | 173.94 | 63.74   |
| 1000                  | 50.73                    | 130.36             | 181.09 | 65.98                    | 51.78             | 136.77             | 188.55 | 66.28   |

interaction terms between X-Y and M-X or X-Y stretching internal coordinates in the Urey-Bradley type potential function are not negligibly small.

Though, as explained above, there are contained a few questionable points and the limits of error are uncertain, we may be allowed to conclude that the assignments in Table III and the potential constants in Table II are reasonable.

As the carbon-oxygen stretching potential constant  $K(\text{C}-\text{O})$ , that of nickel carbonyl<sup>10</sup>, 16.02 mdyn./Å, was employed. For this selection the metal-carbon stretching potential constants  $K(\text{M}-\text{X})$  were obtained to be 1.83 and 1.77 mdyn./Å for chromium and molybdenum hexacarbonyls respectively. These metal-carbon

stretching potential constants are a little smaller than that of nickel carbonyl<sup>10</sup>, 2.12 mdyn./Å, and this fact is in agreement with the study by Giacometti<sup>10</sup> who suggested that the shortening of chromium-carbon bond is smaller than that of nickel-carbon bond in the metal carbonyls. The values of the metal-carbon stretching potential constant, although many authors<sup>10, 11</sup> have discussed the evidence of partial double bond character in such coordination compounds of various symmetry as these metal carbonyls, are nearly equal to those of Si-C and Cr-Cl bonds of tetramethylsilane<sup>12</sup> and chromyl

10) G. Giacometti, *ibid.*, 23, 2068 (1955).

11) See e. g., L. Pauling, "The Nature of the Chemical Bond", Cornell University Press, Ithaca, New York (1939), p. 251.

12) K. Shimizu and H. Murata, private communication.

chloride<sup>13)</sup> (2.72 and 2.56 mdyn./Å respectively), which are considered as single bonds.

The **L** matrices, whose components give the transformation from normal to symmetry coordinates, were calculated and listed in Table VI for chromium hexacarbonyl and Table VII for molybdenum hexacarbonyl.

### Thermodynamic Properties

The heat content, free energy, entropy and heat capacity at constant pressure were calculated for seven temperatures from 273.15 to

1000°K in the rigid rotator-harmonic oscillator approximation using the probable values of the observed wave numbers listed in Table III. The molecular constants used in these computation and the symmetry number are given in Table I, while Table VIII lists the thermodynamic properties.

The authors express their sincere appreciation to Professor R. Tsuchida of Osaka University for helpful suggestions and valuable advice.

Osaka Municipal  
Technical Research Institute  
Kita-ku, Osaka

---

13) H. Stammreich, K. Kawai and Y. Tavares, *Spectrochim. Acta*, 1959, 438.